

Nome: Data:

TAREFA Nº1 - 1ª AVALIACIÓN: DERIVADAS - SOLUCIÓN

1. (10 puntos; 1 punto por cada apartado) **Obtén as derivadas das seguintes funcións e simplifica a solución evitando expoñentes negativos e fraccionarios:**

$$1. \quad f(x) = -\operatorname{sen} \frac{x}{-x^4 + x - 1} \quad ; \quad f'(x) = -\cos \left(\frac{x}{-x^4 + x - 1} \right) \cdot \frac{3x^4 - 1}{(-x^4 + x - 1)^2}$$

$$2. \quad y = \sqrt[3]{(5x+3)^2} \quad ; \quad y' = \frac{10}{3 \sqrt[3]{5x+3}}$$

$$3. \quad f(x) = \sqrt{\sqrt{x}} \quad ; \quad f'(x) = \frac{1}{4} x^{\frac{1}{4}-1} = \frac{1}{4} x^{-\frac{3}{4}} = \frac{1}{4 \sqrt[4]{x^3}}$$

$$4. \quad f(x) = \sqrt{2e^x + \log_2 3x} \quad ; \quad f'(x) = \frac{1}{2\sqrt{2e^x + \log_2 3x}} \left(2e^x + \frac{1}{x \ln 2} \right)$$

$$5. \quad y = \ln \sqrt{\frac{1-x}{1+x}} \quad ; \quad y' = \frac{-1}{1-x^2}$$

$$6. \quad y = x^{\operatorname{sen}(2x-9)} \quad ; \quad y' = \left[2 \cos(2x-9) \ln x + \frac{\operatorname{sen}(2x-9)}{x} \right] x^{\operatorname{sen}(2x-9)}$$

$$7. \quad f(x) = 5x^2 e^x \Rightarrow f'(x) = (5x^2 + 10x)e^x = 5x e^x (x+2)$$

$$8. \quad y = \arcsen(\cos x - x) \quad ; \quad y' = \frac{-\operatorname{sen} x - 1}{\sqrt{1 - (\cos x - x)^2}}$$

$$9. \quad y = (3x+1)^{2x+3} \quad ; \quad y' = \left[2 \ln(3x+1) + \frac{6x+9}{3x+1} \right] (3x+1)^{2x+3}$$

$$10. \quad f(x) = \frac{\log_5 x}{2x-1} \Rightarrow f'(x) = \frac{\frac{2x-1}{x \ln 5} - 2 \log_5 x}{(2x-1)^2} = \frac{2x-1-2x \ln x}{x(2x-1)^2 \ln 5}$$

$$\log_5 x \cdot \ln 5 = \frac{\ln x}{\ln 5} \cdot \ln 5 = \ln x$$