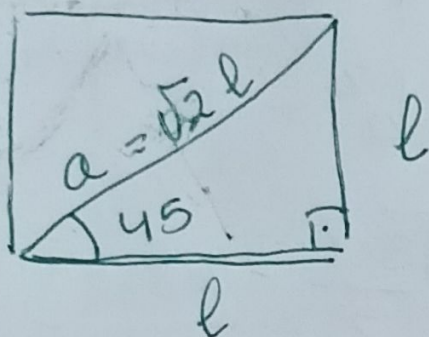


Nombre: \_\_\_\_\_

- No se valorarán ejercicios que sólo presenten el resultado final sin realizar el desarrollo.

1. (3 puntos) Calcular las razones trigonométricas del ángulo de  $45^\circ$ .



Th. pitagoras

$$a^2 = l^2 + l^2$$

$$a = \sqrt{2l^2}$$

$$a = \sqrt{2} \cdot l$$

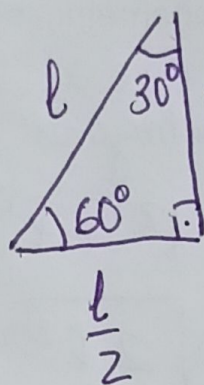
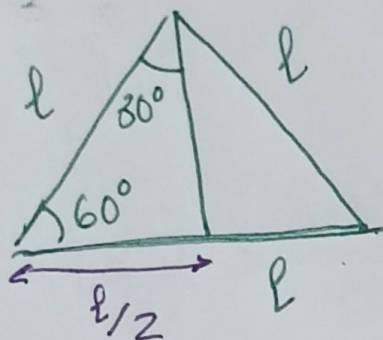
$$\sin 45^\circ = \frac{\text{cat op}}{\text{hip}} = \frac{l}{\sqrt{2}l} = \frac{\sqrt{2}}{2} \Rightarrow \csc 45^\circ = \frac{1}{\sin 45^\circ} = \sqrt{2}$$

$$\cos 45^\circ = \frac{\text{cat cont}}{\text{hip}} = \frac{l}{\sqrt{2}l} = \frac{\sqrt{2}}{2} \Rightarrow \sec 45^\circ = \frac{1}{\cos 45^\circ} = \sqrt{2}$$

$$\tan 45^\circ = \frac{\text{cat op}}{\text{cat cont}} = \frac{l}{l} = 1 \Rightarrow \cotg 45^\circ = \frac{1}{\tan 45^\circ} = 1$$

2. (3 puntos) Calcular las razones trigonométricas del ángulo de  $30^\circ$  y  $60^\circ$ .

### TRIANGULO EQUILATERO



$$b = \frac{\sqrt{3}l}{2}$$

$$l^2 = \frac{l^2}{4} + b^2$$

$$\frac{3l^2}{4} = b^2$$

$$b = \frac{\sqrt{3}l}{2}$$

$$\sin 30^\circ = \frac{\text{Cat op}}{\text{hip}} = \frac{l/2}{l} = \frac{1}{2} \Rightarrow \operatorname{cosec} 30^\circ = \frac{1}{\sin 30^\circ} = 2$$

$$\cos 30^\circ = \frac{\text{Cat cont}}{\text{hip}} = \frac{\frac{\sqrt{3}l}{2}}{l} = \frac{\sqrt{3}}{2} \Rightarrow \sec 30^\circ = \frac{1}{\cos 30^\circ} = \frac{2\sqrt{3}}{3}$$

$$\operatorname{tg} 30^\circ = \frac{\text{Cat op}}{\text{Cat cont}} = \frac{l/2}{\frac{\sqrt{3}l}{2}} = \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3} \Rightarrow \operatorname{cotg} 30^\circ = \frac{1}{\operatorname{tg} 30^\circ} = \sqrt{3}$$

$$\sin 60^\circ = \frac{\text{Cat op}}{\text{hip}} = \frac{\frac{\sqrt{3}l}{2}}{l} = \frac{\sqrt{3}}{2} \Rightarrow \operatorname{cosec} 60^\circ = \frac{1}{\sin 60^\circ} = \frac{2\sqrt{3}}{3}$$

$$\cos 60^\circ = \frac{\text{Cat cont}}{\text{hip}} = \frac{l/2}{l} = \frac{1}{2} \Rightarrow \sec 60^\circ = \frac{1}{\cos 60^\circ} = 2$$

$$\operatorname{tg} 60^\circ = \frac{\text{Cat op}}{\text{Cat cont}} = \frac{\frac{\sqrt{3}l}{2}}{l/2} = \sqrt{3} \Rightarrow \operatorname{cotg} 60^\circ = \frac{\sqrt{3}}{3}$$

3. (4 puntos) Calcula las restantes razones trigonométricas en los siguientes casos:

a)  $\operatorname{sen} \alpha = \frac{2}{3}$   $\alpha$  es un ángulo del primer cuadrante.

$$\begin{cases} \operatorname{sen} \alpha > 0 \\ \cos \alpha > 0 \end{cases}$$

$$\operatorname{tg} \alpha > 0$$

$$\operatorname{sen}^2 \alpha + \cos^2 \alpha = 1$$

$$\cos \alpha = \pm \sqrt{1 - \operatorname{sen}^2 \alpha}$$

$$\cos \alpha = + \sqrt{\frac{5}{9}} \Rightarrow \cos \alpha = \frac{\sqrt{5}}{3}$$

$$\operatorname{tg} \alpha = \frac{\operatorname{sen} \alpha}{\cos \alpha} = \frac{2/3}{\sqrt{5}/3} = \frac{2\sqrt{5}}{5}$$

b)  $\cos \alpha = \frac{1}{3}$   $\alpha$  es un ángulo del cuarto cuadrante.

$$\begin{cases} \cos \alpha > 0 \\ \operatorname{sen} \alpha < 0 \end{cases}$$

$$\operatorname{tg} \alpha < 0$$

$$\operatorname{sen}^2 \alpha + \cos^2 \alpha = 1$$

$$\operatorname{sen} \alpha = - \sqrt{1 - \cos^2 \alpha}$$

$$\operatorname{sen} \alpha = - \sqrt{\frac{8}{9}}$$

$$\operatorname{sen} \alpha = \frac{-2\sqrt{2}}{3}$$

$$\operatorname{tg} \alpha = \frac{\operatorname{sen} \alpha}{\cos \alpha} = \frac{\frac{-2\sqrt{2}}{3}}{1/3} = -2\sqrt{2}$$

c)  $\operatorname{tg} \alpha = 1$   $\alpha$  está en el tercer cuadrante.

$$\begin{cases} \sin \alpha < 0 \\ \cos \alpha < 0 \end{cases}$$

$$\operatorname{tg} \alpha = 1$$
$$\operatorname{tg}^2 \alpha + 1 = \frac{1}{\cos^2 \alpha} \Rightarrow \cos \alpha = - \frac{1}{\sqrt{1 + \operatorname{tg}^2 \alpha}} = - \frac{1}{\sqrt{2}} = - \frac{\sqrt{2}}{2}$$

$$\operatorname{tg} \alpha = \frac{\sin \alpha}{\cos \alpha}$$

$$\cos \alpha \cdot \operatorname{tg} \alpha = \sin \alpha$$

$$\boxed{\sin \alpha = - \frac{\sqrt{2}}{2}}$$

d)  $\sec \alpha = -5$   $\alpha$  está en el segundo cuadrante.

$$\begin{cases} \sin \alpha > 0 \\ \cos \alpha < 0 \\ \operatorname{tg} \alpha < 0 \end{cases}$$

$$\sec \alpha = -5 \Rightarrow \cos \alpha = -\frac{1}{5}$$

$$1 + \operatorname{tg}^2 \alpha = \sec^2 \alpha$$

$$\operatorname{tg} \alpha = -\sqrt{\sec^2 \alpha - 1}$$

$$\operatorname{tg} \alpha = -\sqrt{24} \Rightarrow \operatorname{tg} \alpha = -2\sqrt{6}$$

$$\operatorname{tg} \alpha = \frac{\sin \alpha}{\cos \alpha} \Rightarrow \sin \alpha = \operatorname{tg} \alpha \cdot \cos \alpha$$
$$\boxed{\sin \alpha = \frac{2\sqrt{6}}{5}}$$