

(4)

$$b) \sin(45^\circ - \alpha) + \sqrt{2} \sin \alpha = 0 \rightarrow \sin 45^\circ \cos \alpha - \cos 45^\circ \sin \alpha + \sqrt{2} \sin \alpha = 0$$

$$\rightarrow \frac{\sqrt{2}}{2} \cos \alpha - \frac{\sqrt{2}}{2} \sin \alpha + \sqrt{2} \sin \alpha = 0 \rightarrow \frac{\sqrt{2}}{2} \cos \alpha - \frac{\sqrt{2}}{2} \sin \alpha = 0 \rightarrow$$

$$\sqrt{2} \cos \alpha - \sqrt{2} \sin \alpha = 0 \rightarrow \sqrt{2} \cos \alpha = \sqrt{2} \sin \alpha \rightarrow \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sin \alpha}{\cos \alpha} \rightarrow$$

$$\tan \alpha = 1 \Rightarrow \alpha = \arctan 1 = 45^\circ \Rightarrow \begin{cases} \alpha_1 = 45^\circ + k360^\circ \\ \alpha_2 = 225^\circ + k360^\circ \end{cases} \quad k \in \mathbb{Z}$$

$180^\circ + 45^\circ = 225^\circ$

$$c) 2 \cos x = 3 \tan x \rightarrow 2 \cos x = 3 \frac{\sin x}{\cos x} \rightarrow 2 \cos^2 x = 3 \sin x \rightarrow 2(1 - \sin^2 x) = 3 \sin x$$

$$\rightarrow 2 - 2 \sin^2 x = 3 \sin x \rightarrow -2 \sin^2 x - 3 \sin x + 2 = 0$$

$$\sin x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4 \cdot (-2) \cdot 2}}{2 \cdot (-2)} = \frac{3 \pm \sqrt{25}}{-4} = \frac{3 \pm 5}{-4}$$

$$\begin{cases} \sin x = \frac{-2}{-4} = \frac{1}{2} & \textcircled{1} \\ \sin x = -2 & \text{No solución} \end{cases}$$

pues $-1 \leq \sin x \leq 1$

Caso 1 $\sin x = \frac{1}{2} \Rightarrow \alpha = \arcsin \frac{1}{2} = 30^\circ \Rightarrow \begin{cases} \alpha_1 = 30^\circ + k360^\circ \\ \alpha_2 = 150^\circ + k360^\circ \end{cases} \quad k \in \mathbb{Z}$

$180^\circ - 30^\circ = 150^\circ$

$$d) 4 \cos(2\alpha) + 3 \cos \alpha = 1 \rightarrow 4(\cos^2 \alpha - \sin^2 \alpha) + 3 \cos \alpha = 1 \rightarrow 4 \cos^2 \alpha - 4 \sin^2 \alpha + 3 \cos \alpha = 1$$

$$\rightarrow 4 \cos^2 \alpha - 4(1 - \cos^2 \alpha) + 3 \cos \alpha = 1 \rightarrow 4 \cos^2 \alpha - 4 + 4 \cos^2 \alpha + 3 \cos \alpha - 1 = 0$$

$$\rightarrow 8 \cos^2 \alpha + 3 \cos \alpha - 5 = 0$$

$$\cos \alpha = \frac{-3 \pm \sqrt{3^2 - 4 \cdot 8 \cdot (-5)}}{2 \cdot 8} = \frac{-3 \pm \sqrt{169}}{16} = \frac{-3 \pm 13}{16} = \begin{cases} \cos \alpha = -1 & \textcircled{1} \\ \cos \alpha = \frac{5}{8} & \textcircled{2} \end{cases}$$

Caso 1 $\cos \alpha = -1 \Rightarrow \alpha = \arccos(-1) = 180^\circ \Rightarrow \begin{cases} \alpha_1 = 180^\circ + k360^\circ \\ \alpha_2 = 180^\circ + k360^\circ \end{cases}$

$360^\circ - 180^\circ = 180^\circ$

Caso 2 $\cos \alpha = \frac{5}{8} \Rightarrow \alpha = \arccos \frac{5}{8} \approx 51^\circ \Rightarrow \begin{cases} \alpha_1 = 51^\circ + k360^\circ \\ \alpha_2 = 309^\circ + k360^\circ \end{cases}$

$360^\circ - 51^\circ = 309^\circ$

SOLUCIONES

$$\begin{aligned} \alpha_1 &= 51^\circ + k360^\circ \\ \alpha_2 &= 180^\circ + k360^\circ \\ \alpha_3 &= 309^\circ + k360^\circ \end{aligned} \quad k \in \mathbb{Z}$$