

Soluções do 3º ESO - 23/03/2020

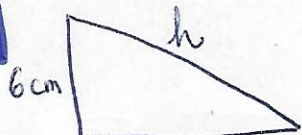
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Aplicando o Teorema de Pitágoras:

$$13^2 = 6^2 + c^2 \Leftrightarrow [c = \sqrt{13^2 - 6^2} = \sqrt{108} = 10,39 \text{ cm}]$$

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$$\left. \begin{array}{l} c_1 = 6 \text{ cm} \\ c_2 - c_1 = 2 \text{ cm} \end{array} \right\} \Leftrightarrow c_2 = 8 \text{ cm}$$

Por Pitágoras: $h^2 = 6^2 + 8^2 \Leftrightarrow h^2 = 100 \Leftrightarrow$

$$\boxed{h = 10 \text{ cm}}$$

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Se cumples o Teorema de Pitágoras son triángulos rectángulos:

a) 5 cm, 12 cm, 13 cm

* Sempre o lado de maior longitude será (se é un triángulo rectángulo) a hipotenusa.

$$13^2 = 5^2 + 12^2 \Leftrightarrow 169 = 25 + 144 \Leftrightarrow 169 = 169$$

Como cumpre o Teorema de Pitágoras é rectángulo

b) 6 cm, 8 cm e 12 cm

$$12^2 = 6^2 + 8^2 \Leftrightarrow 144 = 36 + 64 \Leftrightarrow 144 \neq 100$$

Non cumpre, non é triángulo rectángulo.

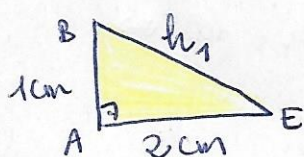
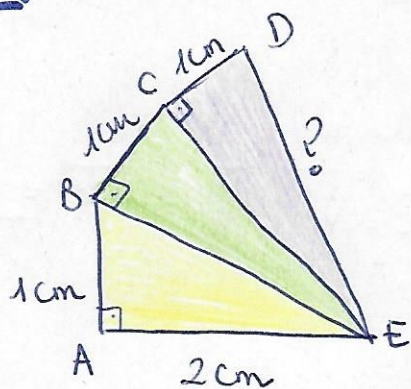
c) 5 cm, 6 cm e $\sqrt{61}$ cm

$$(\sqrt{61})^2 = 6^2 + 5^2 \Leftrightarrow 61 = 36 + 25 \Leftrightarrow 61 = 61$$

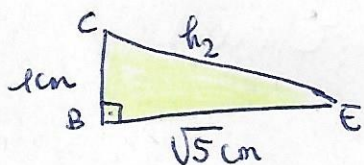
Como cumpre o Teorema de Pitágoras é rectángulo.

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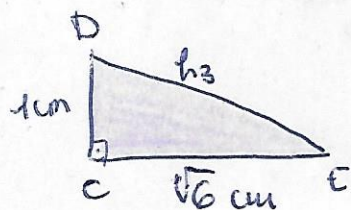
a)



$$h_1 = \sqrt{1^2 + 2^2} = \sqrt{5} \text{ cm}$$



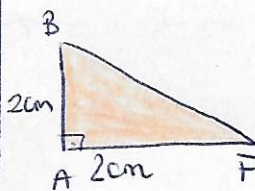
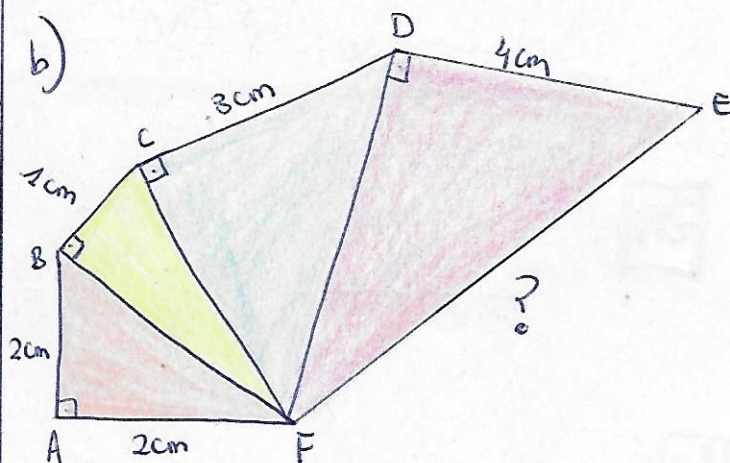
$$h_2 = \sqrt{(\sqrt{5})^2 + 1^2} = \sqrt{6} \text{ cm}$$



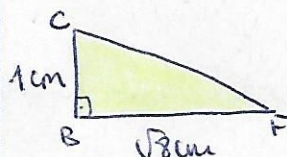
$$h_3 = \sqrt{(\sqrt{6})^2 + 1^2} = \sqrt{7} \text{ cm}$$

Sol: $\sqrt{7} \text{ cm}$.

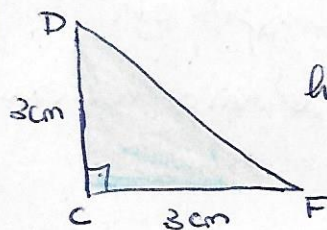
b)



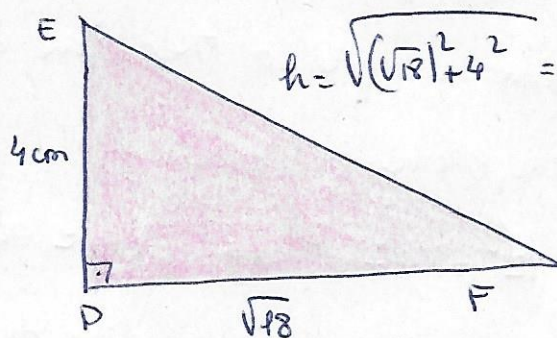
$$h_1 = \sqrt{2^2 + 2^2} = \sqrt{8} \text{ cm}$$



$$h_2 = \sqrt{(\sqrt{8})^2 + 1^2} = 3 \text{ cm}$$



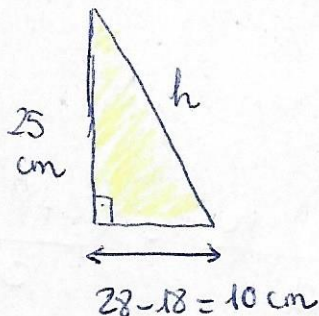
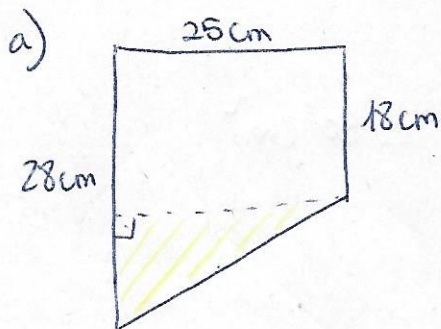
$$h_3 = \sqrt{3^2 + 3^2} = \sqrt{18} \text{ cm}$$



$$h = \sqrt{(\sqrt{18})^2 + 4^2} = \sqrt{34} \text{ cm}$$

Sol: $\sqrt{34} \text{ cm}$

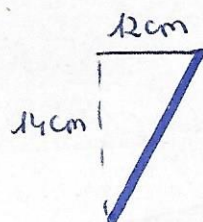
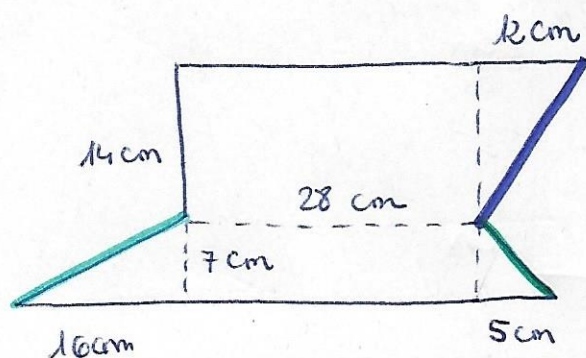
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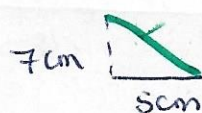
$$h = \sqrt{25^2 + 10^2} = \sqrt{725} \approx 26.93 \text{ cm}$$

Perímetro = $25 + 18 + 26.93 + 28 = \underline{\underline{97.93 \text{ cm}}}$.

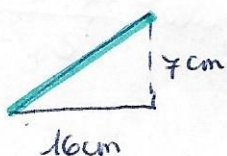
b)



$$h = \sqrt{12^2 + 14^2} = \sqrt{340} \text{ cm} = 18.44 \text{ cm}$$



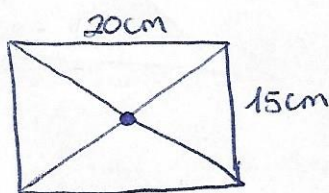
$$h = \sqrt{7^2 + 5^2} = \sqrt{74} \text{ cm} = 8.60 \text{ cm}$$



$$h = \sqrt{16^2 + 7^2} = \sqrt{305} \text{ cm} \approx 17.46 \text{ cm}$$

Perímetro = $\sqrt{305} + 14 + 28 + 12 + \sqrt{340} + \sqrt{74} + 5 + 28 + 16 = \underline{\underline{147.51 \text{ cm}}}$

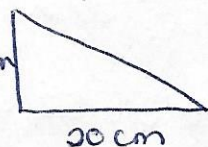
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O retângulo está inscrito na circunferência.
As diagonais do retângulo cortam-se no ponto médio que coincide ao centro da circunferência.

Calculamos a diagonal do retângulo:

$$d = \sqrt{15^2 + 20^2} = 25 \text{ cm}$$



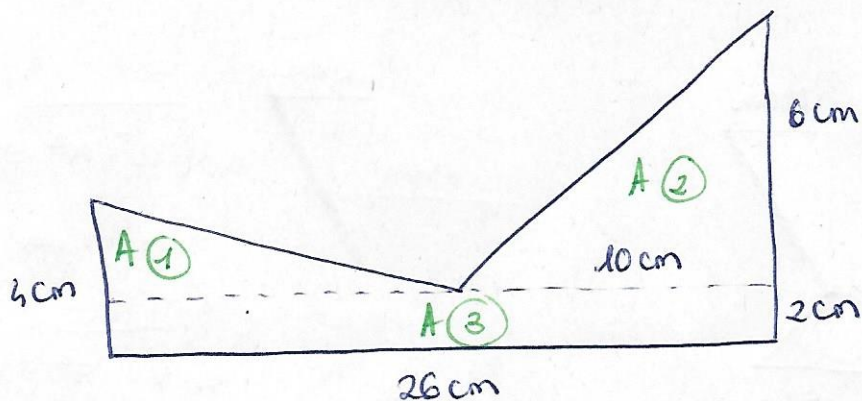
Por tanto o raio mede : $r = \frac{d}{2} = \frac{25}{2} = \underline{\underline{12.5 \text{ cm}}}$.

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$$a) A_{\text{trapezio}} = \frac{(B+b) \cdot h}{2} = \frac{(12+8) \cdot 5}{2} = 50 \text{ cm}^2$$

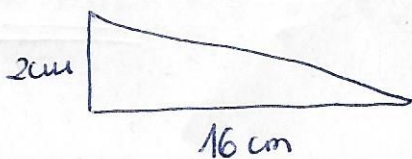
$$b) A_{\text{rombo}} = \frac{D \cdot d}{2} = \frac{12 \cdot 9}{2} = 54 \text{ cm}^2$$

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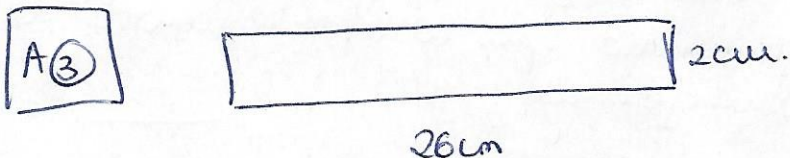
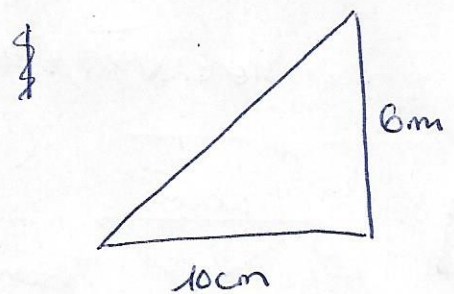


$$A_{\text{rea figura}} = A(1) + A(2) + A(3)$$

$$A(1) \quad A_{\text{triângulo}} = \frac{16 \cdot 2}{2} = 16 \text{ cm}^2$$



$$A(2) \quad A_{\text{triângulo}} = \frac{10 \cdot 6}{2} = 30 \text{ cm}^2$$



$$A_{\text{rectângulo}} = 26 \cdot 2 = 52 \text{ cm}^2$$

$$A_{\text{rea figura}} = 16 + 30 + 52 = \underline{\underline{98 \text{ cm}^2}}$$